

Chapter 5 Analytic Trigonometry

QW: What does analytic mean?

an·a·lyt·ic

[.ənəˈlɪdɪk] 

ADJECTIVE

1. another term for [analytical](#).

- [logic](#)

true by virtue of the meaning of the words or concepts used to express it, so that its denial would be a self-contradiction. Compare with [synthetic](#).

- [linguistics](#)

(of a language) tending not to alter the form of its words and to use word order rather than inflection or agglutination to express grammatical structure. Often contrasted with [synthetic](#).

On a notecard, you need to copy down all the trigonometric identities for sections:

5.1

5.4

5.5

(Also in Chapter summary)

You will use this notecard throughout the chapter. Since some will have to be memorized, we will make a new one for the test.

FUNDAMENTAL TRIGONOMETRIC IDENTITIES

Reciprocal Identities

$$\sin u = \frac{1}{\csc u}$$

$$\cos u = \frac{1}{\sec u}$$

$$\tan u = \frac{1}{\cot u}$$

$$\csc u = \frac{1}{\sin u}$$

$$\sec u = \frac{1}{\cos u}$$

$$\cot u = \frac{1}{\tan u}$$

FUNDAMENTAL TRIGONOMETRIC IDENTITIES

Quotient Identities

$$\tan u = \frac{\sin u}{\cos u}$$

$$\cot u = \frac{\cos u}{\sin u}$$

FUNDAMENTAL TRIGONOMETRIC IDENTITIES

*****Pythagorean Identities*****

$$\sin^2 u + \cos^2 u = 1$$

$$1 + \tan^2 u = \sec^2 u \quad \text{sec}^2 u - 1 = \tan^2 u$$

$$1 + \cot^2 u = \csc^2 u$$

FUNDAMENTAL TRIGONOMETRIC IDENTITIES

Cofunction Identities

$$\sin\left(\frac{\pi}{2} - u\right) = \cos u$$

$$\cos\left(\frac{\pi}{2} - u\right) = \sin u$$

$$\tan\left(\frac{\pi}{2} - u\right) = \cot u$$

$$\cot\left(\frac{\pi}{2} - u\right) = \tan u$$

$$\sec\left(\frac{\pi}{2} - u\right) = \csc u$$

$$\csc\left(\frac{\pi}{2} - u\right) = \sec u$$

FUNDAMENTAL TRIGONOMETRIC IDENTITIES

Even/Odd Identities

$$\sin(-u) = -\sin u \quad \cos(-u) = \cos u \quad \tan(-u) = -\tan u$$

$$\csc(-u) = -\csc u \quad \sec(-u) = \sec u \quad \cot(-u) = -\cot u$$

Simplify:

$$\tan x \csc x$$

$$\frac{\cancel{\sin x}}{\cos x} \cdot \frac{1}{\cancel{\sin x}}$$

$$\frac{1}{\cos x}$$

$$\sec x$$

Simplify:

$$\cos^2 x (\sec^2 x - 1)$$

$$\cos^2 x (\tan^2 x)$$

$$\cancel{\cos^2 x} \left(\frac{\sin^2 x}{\cancel{\cos^2 x}} \right)$$

$$\sin^2 x$$

$$1 + \tan^2 u = \sec^2 u$$

Simplify:

$$\sin x \cos^2 x - \sin x$$

$$\sin x (\cos^2 x - 1)$$

$$\sin x (-\sin^2 x)$$

$$-\sin^3 x$$

$$\sin^2 u + \cos^2 u = 1$$

$$\cos^2 u - 1 = -\sin^2 u$$

Simplify:

$$\sec^2 x (1 - \sin^2 x)$$

$$\begin{aligned} & \sec^2 x (\cos^2 x) \\ & \frac{1}{\cancel{\cos^2 x}} \cdot \frac{\cancel{\cos^2 x}}{1} \\ & \quad | \end{aligned}$$

Factor

a. $4 \tan^2 \theta + \tan \theta - 3$

$$(4 \tan \theta - 3)(\tan \theta + 1)$$

b. $1 - \cos^2 x$

$$(4 \tan \theta - 3)(\tan \theta + 1)$$

$$(2 \csc \theta - 3)(\csc \theta - 2)$$

c. $2 \csc^2 \theta - 7 \csc \theta + 6$

d. $\sec^2 x + 3 \tan x + 1$

$1 + \tan^2 u = \sec^2 u$

$1 + \tan^2 x + 3 \tan x + 1$

$\tan^2 x + 3 \tan x + 2$

$$(\tan x + 1)(\tan x + 2)$$

Simplify: $\frac{\csc^2 x - 1}{\csc x - 1}$

$$\frac{(\cancel{\csc x - 1})(\csc x + 1)}{\cancel{\csc x - 1}}$$
$$\csc x + 1$$

Rewrite $\frac{\cos^2 y}{1 - \sin y}$ so that it is not in fractional form

$$\frac{1 - \sin^2 y}{1 - \sin y}$$

$$\sin^2 u + \cos^2 u = 1$$

$$\frac{(1 - \sin y)(1 + \sin y)}{1 - \sin y}$$
$$1 + \sin y$$

Use the substitution $x = 5 \sin \theta$, $0 < \theta < \frac{\pi}{2}$ to write

$\sqrt{25 - x^2}$ as a trigonometric function of θ

Summarize the major points of the lesson

Essential Question: How do you rewrite trigonometric expressions in order to simplify and evaluate trigonometric functions?

