Solving Exponential Equations

• Take a logarithm

Solving Exponential Equations

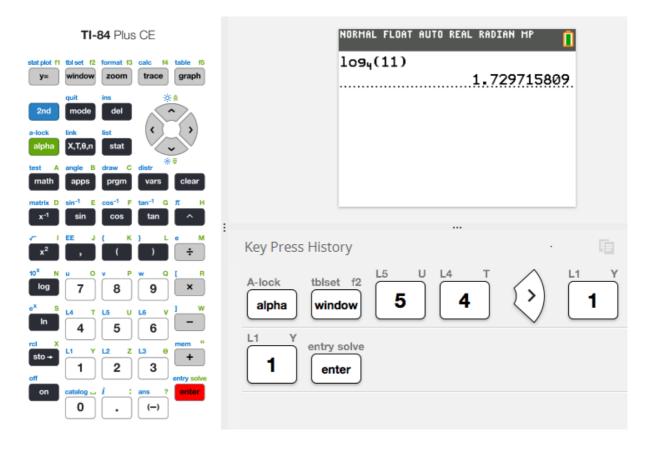
Take a logarithm

Example: Solve
$$4^x = 11$$

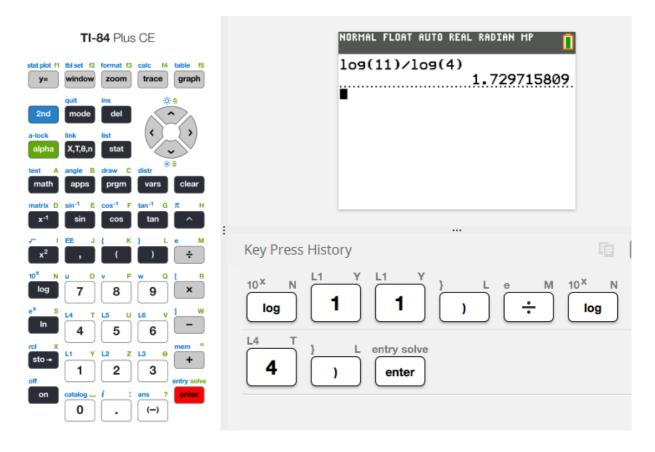
Always take the log of the number that is being raised to the power. Like 4^x

$$\log_4 4^x = \log_4 11$$
 $\log_4 4^x = x$ Use calculator to solve
 $x=1.730$ How to use calculator is on next page

Newer Calculator



Older Calculator



Try these:

$$7^{9x} = 15$$

Do the same method. Find the log on each side.

$$\log_{7} 7^{9x} = \log_{7} 15$$

$$\log_{7} 7^{9x} = 9x$$

$$9x = 1.392$$
Solve for x
$$\frac{9x}{9} = \frac{1.392}{9}$$

$$x = 0.155$$

Always isolate what is being raised to the power first.

$$4e^{-0.3x} - 7 = 13$$
Add 7 to each side
 $4e^{-0.3x} = 20$
Divide by 4
 $e^{-0.3x} = 5$
Take natural log on each side
 $\ln e^{-0.3x} = \ln 5$
 $-0.3x = 1.609$
Divide by -0.3 on each side
 $x=-5.365$

$$4 \cdot 2^{b+8} = 33$$
get 2^{b} by itself

 $2^{b+8} = \frac{33}{4}$ Divide by 4 on each side

 $2^{b+8} = 8.25$
 $\log_2 2^{b+8} = \log_2 8.25$
 $b+8 = 3.044$ Take the log

 $b=3.044-8$ Solve for b

 $b=-4.956$

$$4 \cdot 2^{b+8} = 33$$
get 2^{b} by itself
$$2^{b+8} = \frac{33}{4}$$
Divide by 4 on each side
$$2^{b+8} = 8.25$$

$$\log_{2} 2^{b+8} = \log_{2} 8.25$$

$$\log_{2} 2^{b+8} = \log_{2} 8.25$$

$$n = 11.763$$

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Class work:

SOLVING EXPONENTIAL EQUATIONS Solve the equation.

12.
$$8^x = 20$$

$$11^{5x} = 33$$

18.
$$10^{3x} + 4 = 9$$

13.
$$e^{-x} = 5$$

16.
$$7^{6x} = 12$$

19.
$$-3e^{2x} + 16 = 5$$

14.
$$7^{3x} = 18$$

17.
$$4e^{-2x} = 17$$

20.
$$0.5^x - 0.25 = 4$$